

# Numerical Studies of Heat Transfer of Flue Gases in a Narrow Channel with an Improved Heat Exchange Surface

Rakhimjan Babakhodjaev<sup>1</sup>, Nazim Tashbaev<sup>1</sup>, Jonreed Mirzaev<sup>1</sup> and Bakhran Umarov<sup>2</sup>

<sup>1</sup>Heat power engineering and nuclear power plants Department, Tashkent State Technical University named after Islam Karimov, Universitetskaya Str. 2, 100095 Tashkent, Uzbekistan

<sup>2</sup>Senior Lecturer at the Department of Physical Chemistry, Mirzo Ulugbek National University of Uzbekistan, Universitetskaya Str. 4, 100174 Tashkent, Uzbekistan

rachimjan@mail.ru, confgtu@mail.ru, rachimjan@mail.ru, confgtu@mail.ru

**Keywords:** Channel, Spherical Dimples, Protrusions, Heat Transfer Surface, Flow Turbulization.

**Abstract:** This article presents the results of a study of heat transfer on surfaces with spherical depressions. It provides a rationale for the relevance of the study and a brief overview of previously conducted studies. It specifies the factors that affect the intensity of heat transfer, and explains the mechanism of flow turbulence in a channel with spherical depressions and protrusions. It displays data that determine the parameters that are directly or indirectly included in the similarity criteria, initial and boundary conditions, as well as the geometric and thermal characteristics necessary to create a mathematical model. The mathematical model of heat exchange in channels with an improved heat exchange surface with applied spherical depressions and protrusions is considered, allowing to estimate the influence of the presence of local turbulent areas on the channel surfaces on the Nusselt number in comparison with a similar channel with smooth surfaces. Also, the results of numerical studies on the influence of turbulence on heat exchange characteristics of channels with an improved heat exchange surface are presented in the form of graphs.

## 1 INTRODUCTION

One of the main tasks of heat engineering for many years remains the task of studying the flow of viscous liquid and heat exchange in channels with spherical depressions and protrusions applied to the heat exchange surface. The practical significance of these studies is associated with the intensification of heat exchange in surface heat exchangers.

One of the solutions for increasing the efficiency of heat-using equipment is to increase heat transfer (heat transfer) from one heat carrier to another. This goal is achieved by various methods and techniques. The most commonly used method is turbulization of the heat carrier flow. With turbulized flow of liquid or gas, heat transfer is much more intense than with laminar flow. Turbulization of the flow can be achieved by using various devices located on the heat exchange surfaces. Fins of various shapes, nozzles, artificial roughness and much more can be used as turbulators. It should be borne in mind that the use of turbulators, although it helps to increase the

efficiency of heat transfer, leads to an increase in resistance, and therefore to an increase in the pressure drop of the flow.

## 2 MATERIALS AND METHODS

To intensify heat exchange in channels with flat heat exchange surfaces, a method of flow turbulization is often used by applying spherical and other forms of irregularities to the heat exchange surface [1]-[4].

The use of turbulizing surfaces in the form of various dimples and protrusions is one of the methods of intensifying heat exchange in narrow channels [5]-[7].

The flow and heat exchange modes in channels, especially in narrow channels with turbulizing surfaces, differ from similar processes occurring in smooth channels.

The main factor influencing the intensity of heat exchange in such channels is the presence of spherical

depressions and protrusions on the heat exchange surfaces, which serve to turbulize the flow.

When coolants flow around spherical depressions and protrusions located on the heat exchange surface, dynamic vortex structures arise, which are observed both in laminar and turbulent flow regimes. The resulting vortices contribute to an increase in heat transfer [8], [9].

When constructing a model and processing the experimental results in the form of criteria formulas, it is necessary to specify the determining parameters that are directly or indirectly included in the similarity criteria. In stationary problems of convective heat exchange, the determining parameters include:

- $R_0$  – determines (characteristic) size of the heat exchange region;
- $T_0$  – determines (characteristic) temperature in the heat exchange region;
- $w_0$  – determines velocity.

When creating a mathematical model of heat exchange on a surface with applied spherical depressions and protrusions, the geometric values of the depressions and protrusions were changed in the following ranges:  $h$  is the depth of the depression 0.1-20 mm;  $S_x$  is the longitudinal step, 10-50 mm;  $S_y$  is the transverse step, 5-35 mm;  $\gamma$  is the density of application of depressions and protrusions, 20-70%, and the thermophysical parameters of the flow took values in the following ranges:  $Re$  – 1000-50000;  $\nu$  is the kinematic viscosity of flue gases  $112 \times 106 \text{ m}^2/\text{sec}$ ;  $\omega_0$  is the flow velocity of flue gases, 1-20 m/sec;  $a$  is the coefficient of thermal diffusivity of flue gases,  $= 183.2 \text{ m}^2/\text{sec}$ , the geometric parameters of the channel were adopted as follows:  $d_k$  is the channel diameter,  $d_k = 4f/\Pi$ ;  $H$  – 30-60 mm;  $l$  – 35-85 mm;  $d_{\pi}$  – recess diameter, 10-30 mm.

The modeling is based on numerical calculations based on the dependence proposed in [10], [11], [12]:

$$\frac{Nu}{Nu_0} = (1 + 0,50 \gamma) K_f, \quad (1)$$

where  $K_f = \pi h^2 / 2 S_x S_z$ .

For a smooth surface, heat transfer is calculated using the following formula:

$$Nu_0 = 0.024 Re_0^{0.8} Pr^0, \quad (2)$$

where  $Pr = 0,61$ , criteria  $Re_0 = \omega_0 d / \nu$ .

Having determined  $Nu_0$  from (1), we find  $Nu$  and then  $\alpha$ , the heat transfer coefficient for the improved surface:

$$\alpha_1 = Nu \lambda_{gas} / d_k, \quad (3)$$

where  $\lambda_{gas} = 8.27 \cdot 10^{-2}$ , W/m deg, is the thermal conductivity coefficient of flue gases at  $t_{gas} = 700^\circ\text{C}$ . In addition, calculations were carried out using the empirical equation proposed in [12], where the channel height  $H$  is taken into account in the geometric coefficient.

$$\frac{Nu}{Nu_0} = 1 + 4,4 [\gamma(h/D)]^{0,8} / (H/D)^{0,6}, \quad (4)$$

where  $H$  is the channel height, m.

The analysis of (1) and (4) showed that (1) does not take into account the depression diameter  $D$ , while (4) does not consider the density of the applied depressions  $\gamma$ . Considering the significance of the parameters  $D$  and  $\gamma$ , the authors proposed the following (5) for calculating the heat transfer intensity, which accounts for the influence of both of these parameters.

$$\frac{Nu}{Nu_0} = 1 + (\gamma K_{f1}) / Nu_0, \quad (5)$$

where  $K_{f1} = (\pi(2hr - h^2)) / (S_x S_z)$ ,  
where  $r$  – radius of the depression, m.

### 3 RESULTS AND DISCUSSION

Numerical calculations for given geometric and thermophysical parameters yielded the following results, some of which are shown in Figure 1, Figure 2, Figure 3, Figure 4, Figure 5, Figure 6.

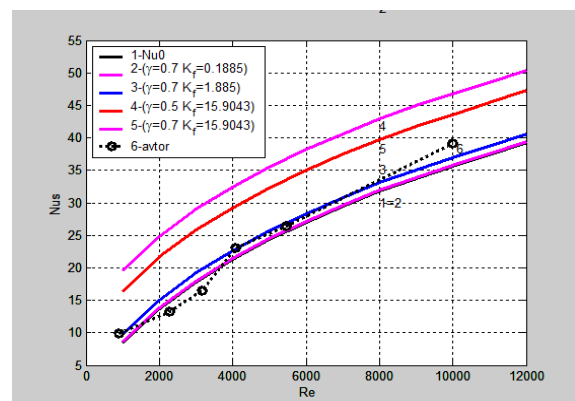


Figure 1: Dependence of the Nusselt number  $Nu$  on the Reynolds number  $Re$  at various values of  $\gamma$ .

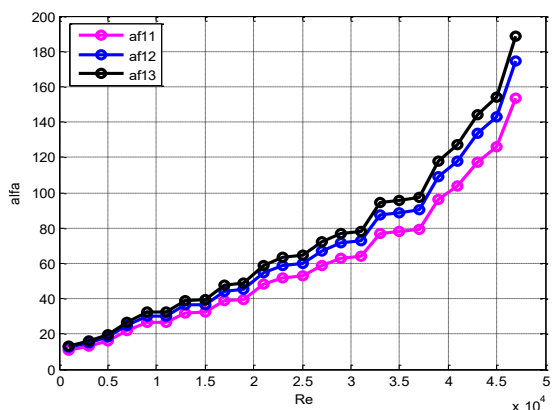


Figure 2: Dependence of the heat transfer coefficient  $\alpha$  on the Reynolds number  $Re$  for different values of  $\gamma$ .

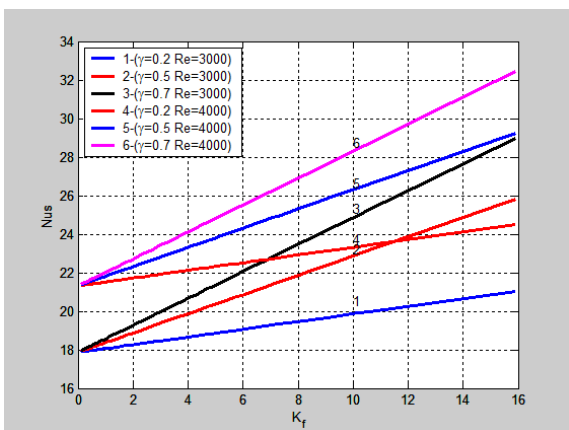


Figure 3: Dependence of the  $\frac{Nu}{Nu_0}$  ratio on the Reynolds number ( $Re$ ) for different values of  $\gamma$  and  $dk$ .

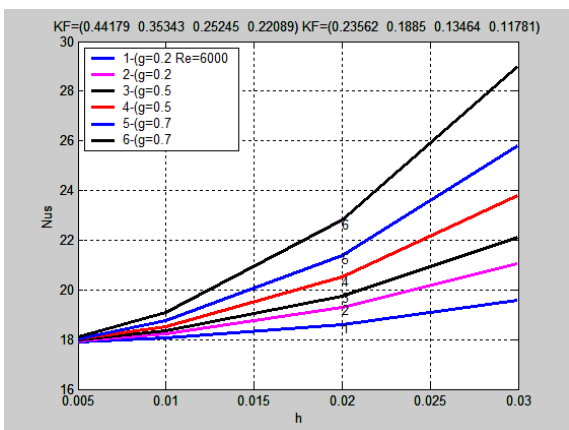


Figure 4: Graph of the dependence of  $\frac{Nu}{Nu_0}$  on  $h$ , the dimple depth, at different dimple densities  $\gamma_m=0.2; 0.5; 0.7$  and at various  $K_f$  values ( $Re=6000$ ).

Analysis of the obtained calculated curves showed that as the depth of the turbulence-inducing dimples and the area of the surface with such dimples increase, the intensity of heat transfer from the heat carrier to the surface also increases. A similar pattern of the influence of dimple depth on heat transfer intensity at different values of the improved (dimpled) surface area fraction is observed for various Reynolds numbers ( $Re$ ).

The analysis of the calculated curves presented in Figure 4 shows that an increase in the density of turbulence-inducing dimples ( $\gamma_m$ ) leads to an increase in heat transfer intensity. Moreover, as the geometric coefficient  $K_f$  increases, the enhancement of heat transfer becomes more significant. It should be noted that the nature of the influence of dimple density on heat transfer intensity remains consistent for different Reynolds numbers ( $Re$ ).

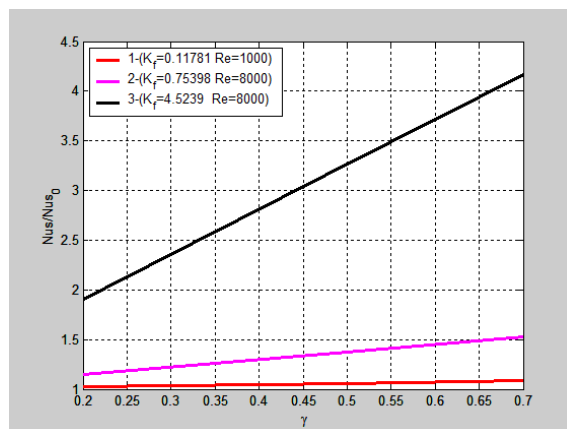


Figure 5: Dependence of  $\frac{Nu}{Nu_0}$  on the dimple density  $\gamma_m$  at different values of  $K_f=0.11781, 0.7539, 4.5239$  ( $Re=1000, 8000$ ).

Figure 6 presents graphs of the calculated values showing the influence of the geometric coefficient  $K_f$  on the intensity of heat transfer. The analysis showed that as the fraction of the surface improved with turbulence-inducing dimples increases, the heat transfer intensity also increases. An increase in the Reynolds number ( $Re$ ) likewise leads to an increase in heat transfer intensity.

Special attention should be paid, when designing heat exchange surfaces with turbulizers, to the parameters of dimple arrangement on the surface — that is, to analyzing the influence of the longitudinal and transverse pitches of the dimples, which determine the dimple density coefficient. The influence of the arrangement parameters (transverse and longitudinal pitches) on the heat transfer intensity was investigated numerically (Figures 7 and 8).

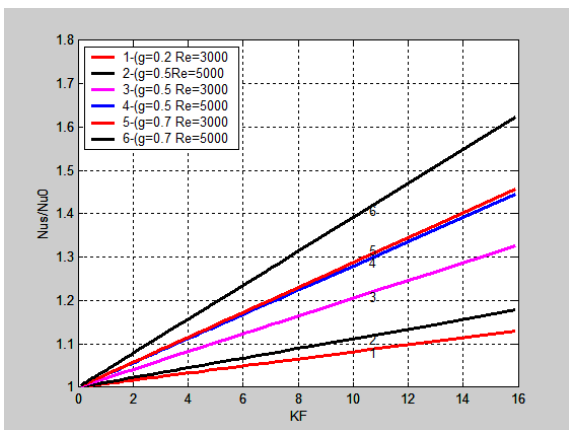


Figure 6: Graph of the dependence of heat transfer intensity  $\frac{Nu}{Nu_0}$  on the geometric coefficient  $K_f$  at different dimple densities  $\gamma = 0.2; 0.5; 0.7$  and  $Re = (3000, 5000)$ .

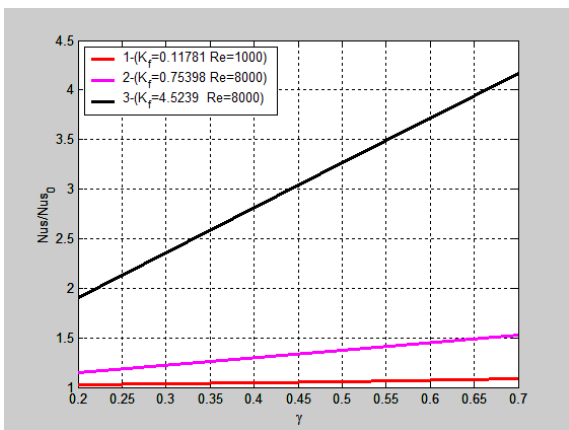


Figure 7: Graph of the dependence of  $\frac{Nu}{Nu_0}$  on  $S_z$  at  $\gamma = 0.2; 0.5; 0.7$  and  $Re = 6000$ .

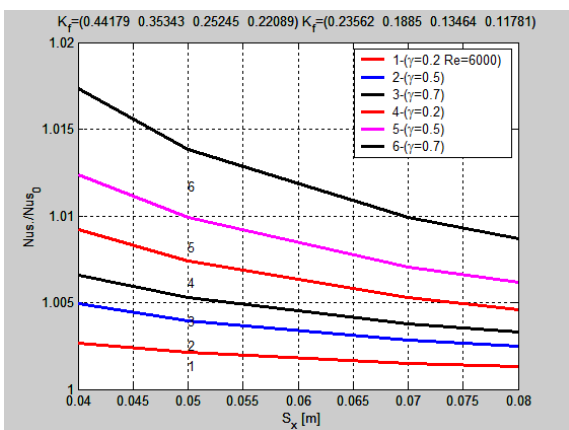


Figure 8: Graph of the dependence of  $\frac{Nu}{Nu_0}$  on  $S_x$  at  $\gamma = 0.2, 0.5, 0.7$  ( $Re = 6000$ ).

The analysis showed that as the geometric parameters of the arrangement of turbulence-inducing depressions increase, the intensity of heat transfer decreases. This is due to the overall reduction of the geometric coefficient  $K_f$  and the decrease in the proportion of the enhanced surface.

The authors conducted a comparative analysis of the results obtained using the proposed (5) with the results of studies by other researchers [11], [12]. Figures 9, 10, and 11 present several graphs illustrating this comparative analysis.

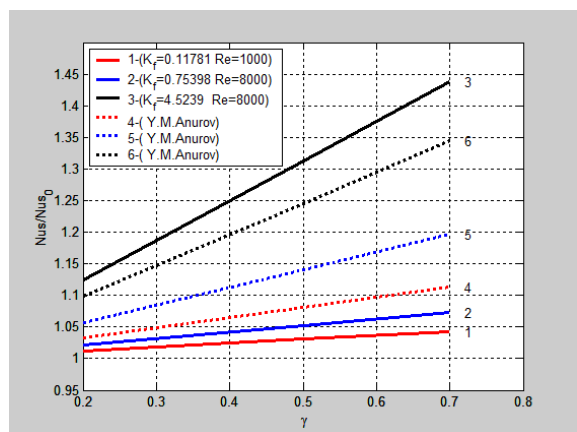


Figure 9: Dependence of the heat transfer intensity  $\frac{Nu}{Nu_0}$  on the density of the applied depressions  $\gamma$ .

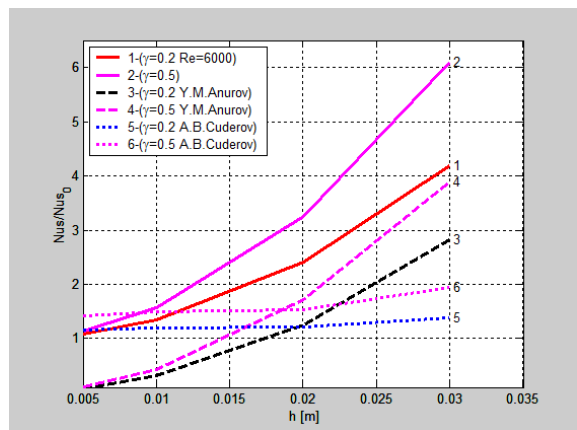


Figure 10: Dependence of the heat transfer intensity  $\frac{Nu}{Nu_0}$  on the depth of the turbulence-inducing depressions  $h$ .

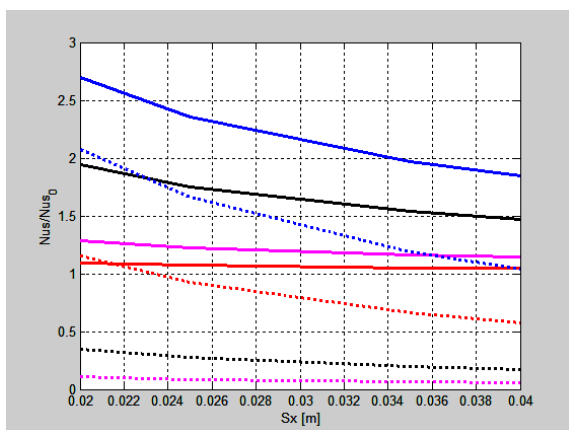


Figure 11: Dependence of the heat transfer intensity  $\frac{Nu_x}{Nu_0}$  on the longitudinal pitch  $S_x$  of the depressions arrangement.

## 4 CONCLUSIONS

The analysis of the obtained dependencies showed that the flow turbulization achieved by applying turbulence-inducing depressions on the heat exchange surface enhances heat transfer. Increasing the depth of the turbulence-inducing depressions ( $h$ ) together with the density of the applied depressions ( $\gamma$ ) contributes to up to a twofold increase in heat transfer, although at certain  $S_x$  values, a slight decrease in heat transfer is observed.

An increase in the density of turbulence-inducing depressions at a constant geometric coefficient ( $K_f$ ) also intensifies heat exchange, though to a lesser extent.

Changes in the geometric dimensions of the depressions likewise affect the heat transfer intensity; with larger  $dk$  values, large vortices form in the depression area, leading to a predictable increase in flow turbulence and consequently enhanced heat transfer. Overall, flow turbulization using depressions allows for an increase in heat exchange intensity, which in turn can reduce the initial consumption of organic fuel.

## REFERENCES

- [1] A. S. Vlasenko, Increasing the efficiency of heat exchangers by intensifying heat transfer on surfaces with spherical depressions, Cand. Sci. dissertation, Moscow, Russia, 2011.
- [2] R. Deeb, "Impact of dimple geometry modifications on flow separation, reattachment, and heat transfer over a dimpled plate," *Appl. Therm. Eng.*, vol. 280, pt. 2, p. 128081, Dec. 2025.
- [3] S. A. Isaev, A. I. Leontiev, N. V. Kornev, E. Hassel, and Ya. P. Chudnovsky, "Heat transfer enhancement for laminar and turbulent flows in a narrow channel with single-row oval dimples," *High Temp.*, vol. 53, no. 3, pp. 375–386, 2015.
- [4] I. I. Borisov, A. A. Khalatov, S. Kobzar, and B. Glezer, "Comparison of thermohydraulic characteristics of two types of pitted surfaces," in *Proc. ASME Turbo Expo*, 2004, doi: 10.1115/GT2004-542041.
- [5] M. D. Selezneva, S. A. Knyazev, A. A. Klyus, and V. V. Seroshtanov, "Heat transfer enhancement in a single oval-trench dimple on a plate with varying inclination angle," *Aerosp. Eng. Technol.*, vol. 1, no. 4, pp. 30–41, 2023.
- [6] L. Eshkuvatov, R. Babakhodjayev, and N. Tashbayev, "Intensification of heat transfer during condensation of water vapor on a vertical tube," *E3S Web Conf.*, vol. 434, art. 01012, 2023, doi: 10.1051/e3sconf/202343401012.
- [7] Y. P. Chudnovsky and A. Kozlov, Development and Field Trial of Dimpled-Tube Technology for Chemical Industry Process Heaters. U.S. Department of Energy, 2006.
- [8] A. M. Bektursynov, S. B. Berdimbetov, and N. K. Yusupova, "Intensification of heat transfer in the intertube space of shell-and-tube heat exchangers," *Universum: Tech. Sci.*, no. 6(99), 2022.
- [9] N. T. Tashbaev, R. P. Babakhodzhaev, K. A. Tokhtakhunov, and A. A. Sadiyev, "Study of hydrodynamic characteristics of regenerator packing," *Probl. Energy Resour. Saving*, no. 1–2, pp. 240, 2017.
- [10] Yu. F. Gortyshov, I. A. Popov, V. V. Olimpiev, A. V. Shchelchikov, and S. I. Kaskov, Heat and Hydraulic Efficiency of Methods for Heat Transfer Intensification in Channels of Heat Exchange Equipment. Kazan, Russia: Center for Innovation Technologies, 2009.
- [11] A. A. Khalatov, I. I. Borisov, and S. V. Shevtsov, Heat and Mass Transfer and Thermal-Hydraulic Efficiency of Vortex and Swirling Flows. Kyiv, Ukraine: Institute of Technical Thermophysics NASU, 2005.
- [12] A. V. Sudarev, B. V. Sudarev, and V. V. Kondrat'ev, "Application of three-dimensional relief for heat exchange enhancement in gas-to-gas heat exchangers," in *Proc. 5th Int. Symp. Experimental and Computational Aerothermodynamics of Internal Flows*, Gdansk, Poland, 2001, pp. 607–618.